2023 national curriculum tests

Key stage 2

Mathematics test mark schemes

Paper 1: arithmetic Paper 2: reasoning Paper 3: reasoning



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1. Introduction

The Standards and Testing Agency (STA) is responsible for the development and delivery of statutory tests and assessments. STA is an executive agency of the Department for Education.

The 2023 tests assess the national curriculum. This test has been developed to meet the specification set out in the <u>test framework</u>¹ for mathematics at key stage 2.

A new test and new mark schemes will be produced each year.

Key stage 2 tests are marked by external markers, who receive training to ensure the mark schemes are applied consistently and fairly. The mark schemes are provided to show teachers how the tests are marked. The pupil examples are based on responses gathered from the test trialling process.

Scaled score conversion tables are not included in this document. Conversion tables will be produced as part of the standards maintenance process. <u>Scaled score conversion tables</u>² for the 2023 tests will be published in July 2023. The standards confirmation meeting will take place in June 2023.

2. Structure of the test

The key stage 2 mathematics test comprises:

- Paper 1: arithmetic (40 marks)
- Paper 2: reasoning (35 marks)
- Paper 3: reasoning (35 marks)

3. Content domain coverage

The 2023 test meets the specification in the test framework. Table 1 sets out the areas of the content domain that are assessed in Papers 1, 2 and 3.

The references are taken from the test framework. A question assessing 4C7, for example, sets out to 'multiply two-digit and three-digit numbers by a one-digit number using a formal written layout' and is taken from the year 4 programme of study.

¹ www.gov.uk/government/publications/key-stage-2-mathematics-test-framework

² www.gov.uk/guidance/scaled-scores-at-key-stage-2

Table 1: Content domain coverage of the 2023 key stage 2 mathematics test

Where 2 or more references are given, the primary reference is given first.

Pape	Paper 1: arithmetic Paper 2: reasoning		Paper 1: arithmetic		Pape	r 3: reasoning
Qu.	Content domain reference	Qu.	Content domain reference	Qu.	Content domain reference	
1	3N2b	1	3M4c/4N3b	1	3N3	
2	4C2	2	5N5	2	5N2/5N3a	
3	4C7	3	4P3a/4P3b	3	6P2	
4	4C2	4	3S2	4	5N1/6A3	
5	4C6b	5	6R4/6A5	5	4F7	
6	5C6b	6	4M9/3M9a	6	6N3	
7	5F8/5F10	7	4N5/4N1/6A3	7	3F1c/3F10	
8	4C2	8	4N4b	8	5G2b	
9	4C6b	9	6G5	9	3C6	
10	3C7	10	4C3/3C8	10	5C5d	
11	4C6b	11a	5N1/4N2b	11	4C4	
12	3C1	11b	5N1/4N2b	12	6G3b	
13	4C6b	12	4G2b	13	6C8/6C9	
14	6F5a	13	5F5/4F10a	14a	5F11/5F12	
15	5C7b	14	5G4c/5G4a	14b	5F11/5F12	
16	5F4	15	5F3/6F3	15a	3M4d/3M4f/4M4b	
17	6F9a	16	5C8c/3M4f	15b	3M4f	
18	5F4	17	5C8b/5C7b	16	6C7b/6C8/6C6	
19	5F8/5F10	18	5F4/6F2	17	6F4/6F11	
20	6C7a	19	5C8a/5C6a	18a	5S1/4S1	
21	6F5b	20	6C7a/6C8	18b	6S3/6C8	
22	4F4	21	5M6	19	5M9c/5M9a	
23	6C9	22	4F2/5F4	20	6A1/4M7a	
24	6F9b	23	6R2/6C8	21	6R2	
25	6C7b	24	6S1/6R2	22	6A3/6G2a	
26	5C7b	25a	5C8a/5C6a	23	6F6/6F11	
27	6R2	25b	5M9c/5M5/5F10	_		
28	6F5b	26a	6A2/6C9			
29	6C7a	26b	6A2/6C9			
30	6R2					
31	6F9b					
32	3F4/3C4					
33	6C7b					

34

35

36

6F4

6R2

5F5

4. Explanation of the mark schemes

The marking information for each question is set out in the form of tables (sections 7, 8 and 9).

The purpose of the mark scheme is to define the acceptable answers for each question within the test. Answers other than those listed may be acceptable if they meet the marking criteria.

The '**Qu**.' column on the left-hand side of each table provides a quick reference to the question number and part.

The 'Requirement' column may include two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for an appropriate method
- · examples of some different types of correct answer

The 'Mark' column indicates the total number of marks available for each question part.

The '**Additional guidance**' column indicates alternative acceptable answers and guidance, such as the range of acceptable answers, where necessary. This column may also provide details of specific types of answer which are unacceptable. For most questions, there will be unacceptable answers that are not listed.

5. General marking guidance

5.1 Applying the mark schemes

To ensure consistency of marking, the most frequent procedural queries are listed in section 5.2 along with the action the marker will take. This is followed by further guidance in section 6 relating to marking questions involving money, time and other measures. Unless otherwise specified in the mark scheme, markers will apply these guidelines in all cases.

Recording marks awarded

Pupils' test papers are scanned so that marking can be conducted on screen by trained markers.

For each question, markers record the award of 3, 2, 1 or 0 marks as appropriate, according to the mark scheme criteria. There is provision in the software to record questions not attempted. The software aggregates marks automatically.

5.2 General marking principles

Table 2: General marking principles for all papers

1.	The answer does not closely match any of the examples given in the mark scheme.	Markers will use their judgement to decide whether the answer corresponds with details in the 'Requirement' column of the mark scheme. Reference will also be made to the 'Additional guidance' column.	
2.	The answer is provided in a non- standard way.	Pupils may provide evidence in any form as long as its meaning can be understood. Diagrams, symbols or words are acceptable for explanations or for presenting an answer.	
3.	The correct answer or working has been crossed out or erased and not replaced.	The mark(s) will not be awarded for crossed-out or erased answers or working.	
4.	More than one answer is given.	If all answers given are correct (or a range of answers is given, all of which are correct), the mark(s) will be awarded unless the mark scheme states otherwise. If both correct and incorrect answers are given, the mark(s) will not be awarded unless the mark scheme states otherwise.	
5.	No answer is given in the expected place, but the correct answer is given elsewhere.	Where a pupil has unambiguously indicated the correct answer, the mark(s) will be awarded. In particular, where a word or number is expected, a pupil may meet the requirement by annotating a graph or labelling a diagram elsewhere in the question.	
6.	The answer is correct, but the wrong working is shown.	A correct final answer will be awarded the mark(s).	
7.	The pupil has used alternative notation	No alternative notation is accepted as representing a decimal point in a number, for example, a comma.	
	for a decimal point in a number.	Refer to section 6 for guidance on marking specific types of question.	
8.	The pupil has used a symbol as a thousands separator.	If the pupil has used a comma as a thousands separator (positioned either correctly or incorrectly) and the digits are in the correct order, then the mark(s) will be awarded.	
		If any other symbol, for example, a decimal point or apostrophe, is used, the mark(s) will not be awarded, although method marks may still be available.	

9. The answer in the answer box is wrong	A transcription error occurs when a pupil miscopies their answer from the end of their working into the answer box.
due to a transcription error.	Each part (integer, numerator, denominator) of a mixed number is considered separately when applying transcription error rules.
	Where appropriate, detailed guidance will be given in the mark scheme. For questions with no guidance, marks will only be awarded for a transcription error if the wrong answer is due to:
	 transposed digits in a number (for example, 243 is written as 324)
	OR
	 one digit changed in a number of 4 or more digits (for example, 2,345 is written as 2,845)
	The mark(s) will not be awarded for any other transcription error including:
	 a decimal point positioned incorrectly (for example, 12.34 is written as 1.234 or 1234)
	 a change by a power of 10 (for example, 200 is written as 20 or 2,000)
	 a digit added or removed (for example, 123,456 written as 1233,456 or 12,456)
	a negative sign added or removed
10. The answer is numerically or algebraically equivalent to the	Answers should be given as single values in their simplest form unless the mark scheme states otherwise, for example, for $$ = 536 – 30, the answer 500 + 6 will not be awarded the mark.
answer in the mark scheme.	For integer answers, for example, 20, the answer $\frac{20}{1}$ will be awarded the mark; $\frac{80}{4}$ will not be awarded the mark.
	For decimal answers that include recurring digit(s), there must be an unambiguous indication of the recurring digit(s). For example, for $\frac{1}{6}$, 0.16 or 0.16 will be awarded the mark and for $\frac{1}{7}$, 0.142857 or 0.142857 will be awarded the mark.
	For fraction answers that can be expressed as a mixed number, the fraction paired with the integer must be a proper fraction, for example, $1\frac{6}{4}$ will not be awarded the mark although method marks may still be available.
	Where alternative responses are acceptable, this will be indicated in the 'Additional guidance' column.

11. The answer in the answer box is wrong due to a misread of numbers given in the question.	Misreads are not allowed in Paper 1; the mark(s) will not be awarded.
12. The pupil has not recorded their working beneath the given long multiplication or	If a pupil carries out their working somewhere on the page other than beneath the given question as expected, then the pupil must start by rewriting the original question in order for it to be considered as a formal method.
long division.	Please note that the operation sign does not need to be given for long multiplication, provided the pupil's working shows the intention to multiply.
13. The answer to the long division question expresses a remainder.	If a pupil reaches an integer answer using a formal method with no more than one arithmetic error, for example, 25, then the mark(s) will be awarded for 25 r0 or 25.0, but the mark(s) will not be awarded for an answer of 250
	For answers with a remainder, the remainder must be expressed correctly.
	If a pupil shows a remainder that is the same size as the divisor or larger, for example, a remainder of 28 or 29 when dividing by 28, the mark(s) will not be awarded because the method is incomplete.
	If a pupil reaches a non-integer answer using a formal method with no more than one arithmetic error, for example, when dividing by 28, the pupil reaches the answer 6 r14, then the mark(s) will be awarded for $6\frac{14}{28}$ or 6.5, but the mark(s) will not be awarded for 6 $r\frac{14}{28}$ or 6.14 or 614
14. The long division method involves subtracting chunks of different sizes.	If a pupil's formal method involves subtracting chunks, it is not necessary to show a separate addition of the chunks. If the answer is not the correct total for their chunks, then that is treated as one arithmetic error.
	A method is considered as chunking when the size of the chunks are shown alongside the algorithm.
	It should be noted that this method will only be accepted if all chunks are of different sizes.

15. More than one method is given.	If a pupil gives more than one method, then the intended method is taken as the one which leads to the answer in the answer box or an identified answer elsewhere. If no answer is given, then all methods must be appropriate for the method mark(s) to be awarded.
16. There appears to be a misread of numbers or information given in the question that affects the pupil's working and/or explanation.	This occurs when a pupil misreads a number given in the question and consistently uses a different number that does not alter the original intention or difficulty of the question. For example, if 243 is misread and written as 248, both numbers may be regarded as comparable in difficulty. However, if 243 is misread and written as 245 or 240, the misread number may be regarded as making the question easier. The misread of a number may affect the award of marks. Any misread number must be seen, not implied.
	Where appropriate, detailed guidance will be given in the mark scheme. If no guidance is given, markers will examine each case to decide whether the mark(s) will be awarded.
	The mark(s) will not be awarded if:
	 it is a ONE-mark question there is more than one misread number in a question the mathematics is simplified it is an 'explain' question it is a misread of other information (not numbers) the misread number is the same as any other number in the question
	For TWO-mark questions that have a method mark, one mark will be awarded if an appropriate method is correctly followed through with the misread number to give the correct follow-through answer, provided the mathematics has not been simplified.
	For THREE-mark questions, refer to the additional guidance.
17. A misread or an arithmetic error results in an answer with multiple decimal places.	In some instances, a misread or an arithmetic error in a method leads to an answer with one or more decimal places. In such cases, the method mark(s) will be awarded for an answer that is correctly truncated or rounded provided the method is appropriate and the additional guidance does not specify otherwise. For example, 1.2345 is truncated to 1.2

Table 4: General marking principles for papers 2 and 3 only (reasoning)

18. The pupil has reversed values within a calculation involving subtraction or division.	When values within the calculation are reversed, the mark(s) will only be awarded when the answer corresponds to the correct calculation. For example, if the correct calculation is $12 \div 4$, the method mark(s) may be awarded for $4 \div 12 = 3$, but not for an answer other than 3 Reversed values within a calculation are not acceptable in 'explain' questions.
19. The pupil omits an operation sign within their working.	If the correct sign of +, - , ×, or ÷ for an arithmetic operation is missing, then the mark(s) will only be awarded if the working shown by the pupil is clear enough to indicate that the required operation has been performed. This applies even if the results of the required operation are incorrect. Where carrying or decomposition figures are seen, this is evidence of intention. For example, where the following is seen in working, the layout of the response implies addition or subtraction: 456 123 • if the answer is larger than the greater of the given values, for example, 679, then addition is implied • if the answer is less than the first given value, for example, 323, then subtraction is implied

20. The pupil has used 'an appropriate method'.	For some questions, the mark scheme allows the award of the method mark(s) for 'evidence of an appropriate method', even if the answer is missing or incorrect. Refer to the 'Additional guidance' column where appropriate.
	For the award of the method mark(s) for an appropriate method, there must be evidence of all the steps of the appropriate method (any method that would lead to the correct answer if there were no arithmetic errors and no additional steps).
	This means that, for every step, either:
	 the appropriate calculation to be carried out must be shown
	OR
	 if the calculation has not been written down, the correct answer or correct follow-through answer must be shown
	Where the calculation shown would lead to a correct final answer, even if the processed numbers do not appear to be taken from the question, a method mark may be awarded unless the mark scheme specifies otherwise.
21. The pupil has used a trial and improvement	'Trial and improvement' is regarded as an acceptable method, unless the mark scheme states otherwise.
method.	For a 'trial and improvement' method to be awarded the method mark(s):
	 there must be at least 3 trials, carried out correctly, which all reduce the range in which the answer is known to lie there can be additional trials, which are correctly or incorrectly carried out, and which may not reduce the range in which the answer is known to lie a final answer is not needed, unless the mark scheme states otherwise

22. The answer in the answer box is wrong but the correct answer	Extra working occurs when a pupil writes the correct answer in their working, and then continues to process the information further.
is reached in the working.	When the answer in the answer box is wrong and does not match the answer reached in the working, it is impossible to know why the pupil has written a different answer and it is assumed that extra working has occurred. GMP 9 on transcription errors still applies.
	If the extra working does not contradict the pupil's appropriate method, the method mark(s) will be awarded.
	If the extra working contradicts the pupil's appropriate method, the method mark(s) will not be awarded.
23. The pupil miscopies a value from one part of	There will be instances when a pupil reaches a value in their working, then restarts from a different value.
their method into the next part.	The mark(s) will not be awarded if:
	• it is a ONE-mark question
	 there is more than one miscopy in the working the miscopy does not follow transcription error rules (see GMP 9)
	The method mark(s) will only be awarded if an appropriate
	method is correctly shown using the miscopied number (which must follow transcription error rules).
24. The correct answer is embedded in the working.	
is embedded in the	(which must follow transcription error rules). An embedded answer occurs when a pupil shows the correct answer within their working but then selects the wrong answer from their working as their final answer or leaves the answer box blank. For example, if a pupil shows $2.5 \times 6 = 3 \times 5$ in the last line of their working and writes 5 in the answer box, whereas the correct answer is 3, then
is embedded in the	(which must follow transcription error rules). An embedded answer occurs when a pupil shows the correct answer within their working but then selects the wrong answer from their working as their final answer or leaves the answer box blank. For example, if a pupil shows $2.5 \times 6 = 3 \times 5$ in the last line of their working and writes 5 in the answer box, whereas the correct answer is 3, then this will affect the award of marks. Where appropriate, detailed guidance will be given in the mark scheme. If no guidance is given, markers will examine
is embedded in the	(which must follow transcription error rules). An embedded answer occurs when a pupil shows the correct answer within their working but then selects the wrong answer from their working as their final answer or leaves the answer box blank. For example, if a pupil shows $2.5 \times 6 = 3 \times 5$ in the last line of their working and writes 5 in the answer box, whereas the correct answer is 3, then this will affect the award of marks. Where appropriate, detailed guidance will be given in the mark scheme. If no guidance is given, markers will examine each case to decide whether the mark(s) will be awarded.

25. The phrase 'sight of' is used in the mark scheme.	For some questions, the mark scheme allows the mark(s) to be awarded for sight of a particular number or numbers within a method. Such numbers are the correct answers to partial steps within a method.		
26. The answer correctly follows through from earlier incorrect work.	'Follow-through' marks for an answer will only be awarded when specifically stated in the mark scheme.		
27. The pupil has drawn lines which do not meet at the correct point.	Where the mark scheme states that 'slight inaccuracies in drawing' should be accepted, this means that the mark(s) will be awarded for responses marked within or on a circle of radius 2mm with its centre at the correct point.		
	within the circleon the circleoutside the circle- accepted- accepted- not accepted		

6. Marking specific types of question: summary of additional guidance

6.1 Answers involving money

	Accept	Do not accept
Where the £ sign is given, for example:	£3.20 £7 £7.00	
£3.20, £7 £	Any unambiguous indication of the correct amount, for example: £3.20p £3 20 pence £3 20 £3-20 £3:20 £3:20	Incorrect placement of pounds or pence, for example: £320 £320p Incorrect placement of decimal point or incorrect use or omission of 0 or use of comma as a decimal point, for example: £3.2 £3 200 £32 0 £3-2-0 £3,20
Where the p sign is given, for example: 40p p	40p Any unambiguous indication of the correct amount, for example: £0.40p 0 40p £0-40p 0:40p £0;40p	Incorrect or ambiguous use of pounds or pence or use of comma as a decimal point, for example: 0.40p £40p £0,40p

	Accept		Do not acc	ept
Where a unit is not given, for example:	£3.20 320p	40p £0.40		
£3.20, 40p	Any unambiguous indication of the correct amount, for example:		Incorrect or ambiguous use of pounds or pence or use of comma as a decimal point, for example:	
	£3.20p	£0.40 pence	£320	£40
	£3 20 pence	£0 40p	£320p	£40p
	£3 20	£0-40	£3.2	0.4
	£3-20	£0:40	3.20p	0.40p
	£3:20	£0;40	£3,20	0,40
	£3;20	£.40		£0,40p
	3.20	0.40		20,100
	320	40		
	3 pounds 20			

6.2 Answers involving time

	Accept		Do not	accept
A time interval, for example: 2 hours 30 minutes	indication, for example:		Incorrect or am interval or use	•
			decimal point,	for example: 230
	(0)2h 30min	150	2.3	2.30 min
	(0)2 30	2.5 hours	2.3 hours	2,5 hours
	(0)2-30	$2\frac{1}{2}$ hours	2.3h	2,30
	Digital electronic time, for example: (0)2:30 (0)2;30		2h 3	1 h 90 min

	Accept	Do not accept
A specific time, for example:	(0)8:40 am	
	(0)8:40	
8:40 am, 17:20	twenty to nine	
	Any unambiguous, correct	Incorrect time, for example:
	indication, for example:	8.4 am
	(0)8.40	8.40 pm
	(0)8;40	Incorrect placement of
	0840	separators, spaces, etc. or
	(0)8 40	incorrect use or omission of 0 or use of a comma as a
	(0)8-40	decimal point, for example:
	Unambiguous change to	840
	12 or 24-hour clock, for example:	8:4:0
	17:20 as 5:20 pm or 17:20 pm	8.4
		084
		8,40

6.3 Answers involving measures

	Accept	Do not accept
Where units are given, for example: 8.6 kg kg	8.6 kg Any unambiguous indication of the correct measurement, for example: 8.60 kg	Incorrect or ambiguous use of units or use of comma as a decimal point, for example: 8600 kg
m	8.6000 kg	8 kg 600
	8 kg 600 g	8,60 kg
		8,6000 kg

If a pupil gives an answer with a unit different from the unit in the answer box, then their answer must be equivalent to the correct answer provided, unless otherwise indicated in the mark scheme.

If a pupil leaves the answer box empty but writes the answer elsewhere on the page without any units, then that answer is assumed to have the units given in the answer box, subject to the conditions listed above.

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7. Mark schemes for Paper 1: arithmetic

Qu.	Requirement	Mark	Additional guidance
1	697	1m	
2	6,594	1m	
3	2,808	1m	
4	8,413	1m	
5	240	1m	
6	960	1m	
7	14.753	1m	
8	2,754	1m	
9	50	1m	
10	520	1m	
11	400	1m	
12	6	1m	
13	900	1m	
14	<u>10</u> 63	1m	Accept equivalent fractions or the exact decimal equivalent, e.g. 0.158730 (accept any unambiguous indication of the recurring digits).
			Do not accept rounded or truncated decimals.
15	83	1m	
16	<u>13</u> 16	1m	Accept equivalent fractions or the exact decimal equivalent, e.g. 0.8125
			Do not accept rounded or truncated decimals.
17	0.03	1m	

Qu.	Requirement	Mark	Additional guidance
18	<u>17</u> 18	1m	Accept equivalent fractions or the exact decimal equivalent, e.g. 0.94 (accept any unambiguous indication of the recurring digits).
			Do not accept rounded or truncated decimals.
19	13.375	1m	
20	Award TWO marks for the correct answer of 37,592	Up to 2m	Working must be parried through to reach
	If the answer is incorrect, award ONE mark for the formal method of long multiplication		Working must be carried through to reach a final answer for the award of ONE mark.
	with no more than ONE arithmetic error, e.g. • 508 $\times \frac{74}{2032}$ <u>35560</u>		Do not award any marks if the error is in the place value, e.g. the omission of the zero when multiplying by tens. 508 $\times 74$
	37582 (error) OR • 508 $\times \frac{74}{2032}$ <u>35060</u> (error) <u>37092</u>		2032 3556 (place value error) 5588
21	<u>1</u> 24	1m	Accept equivalent fractions or the exact decimal equivalent, e.g. 0.0416 (accept any unambiguous indication of the recurring digits).
			Do not accept rounded or truncated decimals.
22	2	1m	Accept equivalent fractions.
			Do not accept answers such as $1\frac{7}{7}$
23	78	1m	
24	38.4	1m	

Qu.	Requirement	Mark	Additional guidance
25	Award TWO marks for the correct answer of 13	Up to 2m	
	If the answer is incorrect, award ONE mark for the formal methods of division with no more than ONE arithmetic error, i.e.		Working must be carried through to reach a final answer for the award of ONE mark.
	long division algorithm, e.g.		
	$ \begin{array}{r} 15 r 25 \\ 47 \overline{\smash{\big)}611} \\ - 470 \\ 260 (error) \\ - 235 \\ 25 \\ \end{array} $		
	OR		
	$ \begin{array}{r} 18 (error) \\ 47 \overline{)611} \\ - 470 \\ 141 \\ - 141 \\ - 141 \\ 0 \\ \end{array} \\ 3 \times 47 \\ \end{array} $		
	 short division algorithm, e.g. 1 5r 6 (error) 47 61²⁴1 		Short division methods must be supported by evidence of appropriate carrying figures to indicate the use of a division algorithm, and be a complete method. The carrying figure must be less than the divisor.
26	1,149 r1	1m	Accept equivalent mixed numbers.
	OR		Do not accept 1,149 r $\frac{1}{5}$
	1,149.2		
	OR 1,149 <u>1</u>		
	1,1495		
27	364	1m	Do not accept 364%
28	<u>1</u> 18	1m	Accept equivalent fractions or an exact decimal equivalent, e.g. 0.05
			Do not accept rounded or truncated decimals.

Qu.	Requirement	Mark	Additional guidance
29	Award TWO marks for the correct answer of 224,761	Up to 2m	
	If the answer is incorrect, award ONE mark for the formal method of long multiplication with no more than ONE arithmetic error, e.g. • 5227 $\times \frac{43}{15681}$ $\frac{209080}{214761}$ (error) OR • 5227 $\times \frac{43}{10681}$ (error) $\frac{209080}{219761}$		Working must be carried through to reach a final answer for the award of ONE mark. Do not award any marks if the error is in the place value, e.g. the omission of the zero when multiplying by tens: $5227 \times \frac{43}{15681}$ $\frac{20908}{36589}$ (place value error) 36589
30	171	1m	Do not accept 171%
31	14.8	1m	
32	<u>3</u> 10	1m	Accept equivalent fractions or an exact decimal equivalent, e.g. 0.3
			Do not accept 30%

Qu.	Requirement	Mark	Additional guidance
33	Award TWO marks for the correct answer of 172	Up to 2m	
	If the answer is incorrect, award ONE mark for the formal methods of division with no more than ONE arithmetic error, i.e.		Working must be carried through to reach a final answer for the award of ONE mark.
	long division algorithm, e.g.		
	$ \begin{array}{r} 172 \text{ r } 10 \\ 26 \overline{\smash{\big }4472} \\ - \underline{2600} \\ 1872 \\ - \underline{1820} \\ 52 \\ - \underline{42} \text{ (error)} \\ 10 \\ \end{array} $		
	OR		
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
	• short division algorithm, e.g. $ \begin{array}{r} 1 & 7 & 3 \\ 26 & 44^{18}7^{5}2 \end{array} $		Short division methods must be supported by evidence of appropriate carrying figures to indicate the use of a division algorithm, and be a complete method. The carrying figures must be less than the divisor.
34	2 <u>1</u> OR	1m	Accept equivalent mixed numbers, fractions or an exact decimal equivalent, e.g. 2.083 (accept any unambiguous indication of the recurring digits).
	<u>25</u> 12		Do not accept rounded or truncated decimals.
35	285	1m	Do not accept 285%
36	600	1m	Do not accept $\frac{1800}{3}$

8. Mark schemes for Paper 2: reasoning

Qu.	Requirement	Mark	Additional guidance
1	Award ONE mark for the correct clock circled, as shown: (x,y) = (x,y) = (x,y	1m	Accept alternative unambiguous positive indication of the correct answer.
2	Award ONE mark for the correct order as shown: -10°C -4°C 1°C 3°C 6°C Lowest	1m	Misreads and transcription errors are not allowed. Accept temperatures in reverse order AND the label lowest changed to follow suit.
3	(6,2)	1m	
4	7	1m	

Qu. Requirement Mark 5 Award **ONE** mark for a correct explanation **1**m that demonstrates why Stefan's total number of wheels is incorrect, e.g. Uses 5 cars and 3 motorbikes to show that the total number of wheels cannot be 28 because there are 26 wheels, e.g. • $5 \times 4 = 20$ $3 \times 2 = 6$ 20 + 6 = 26 (not 28) 20 and 6 - he is wrong because you need an extra pair of wheels. because on 5 cars there are 20 wheels but on 3 motorbikes there are 6 wheels so he would need another motorbike to have 28 wheels. • 26 (not 28) OR Uses 3 motorbikes and the total of 28 wheels to show that the number of cars cannot be 5, e.g. 3 motorbikes would have 6 wheels which leaves 22 wheels for the cars. But 22 divided by 4 is five and a half cars, so that can't be possible. OR Uses 5 cars and the total number of 28 wheels to show that the number of motorbikes cannot be 3, e.g. • There are 5 cars with 20 wheels. And there must be 4 motorbikes for him to have 28 wheels, so Stefan is wrong. OR Demonstrates that Stefan would have either two extra wheels or an extra motorbike, e.g. • He is wrong because he has counted 2 more wheels.

Additional guidance

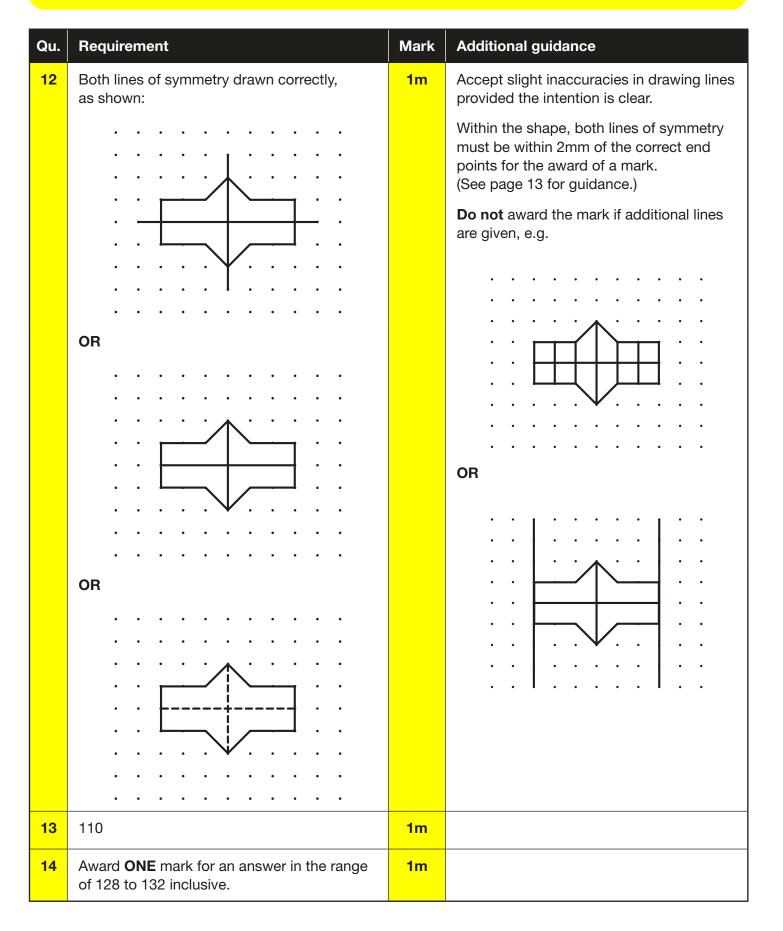
- 20 and 6
- because 3 motorbikes is 6 wheels.
- he is two off the answer.

Do not accept responses that restate the question e.g. 3 motorbikes and 5 cars does not equal 28

Do not accept explanations which include incorrect mathematics or incorrect information relevant to the explanation.

Do not accept vague or incomplete explanations, e.g.

Qu.	Requirement	Mark	Additional guidance
6	£3.61	1m	Refer to section 6.1 on pages 14 and 15 for additional guidance on marking answers involving money.
7	Award ONE mark for the correct order, as shown:	1m	Do not accept 25–
	75 50 25 0 –25		
8	24,400	1m	Do not accept 400
9	Award ONE mark for all three diagrams matched correctly, as shown:	1m	Lines need not touch the diagrams and names, provided the intention is clear.
	circumference diameter		Do not accept a diagram matched to more than one name.
	radius		
10	216	1m	
11 a	20,039	1m	
11b	18,939	1m	



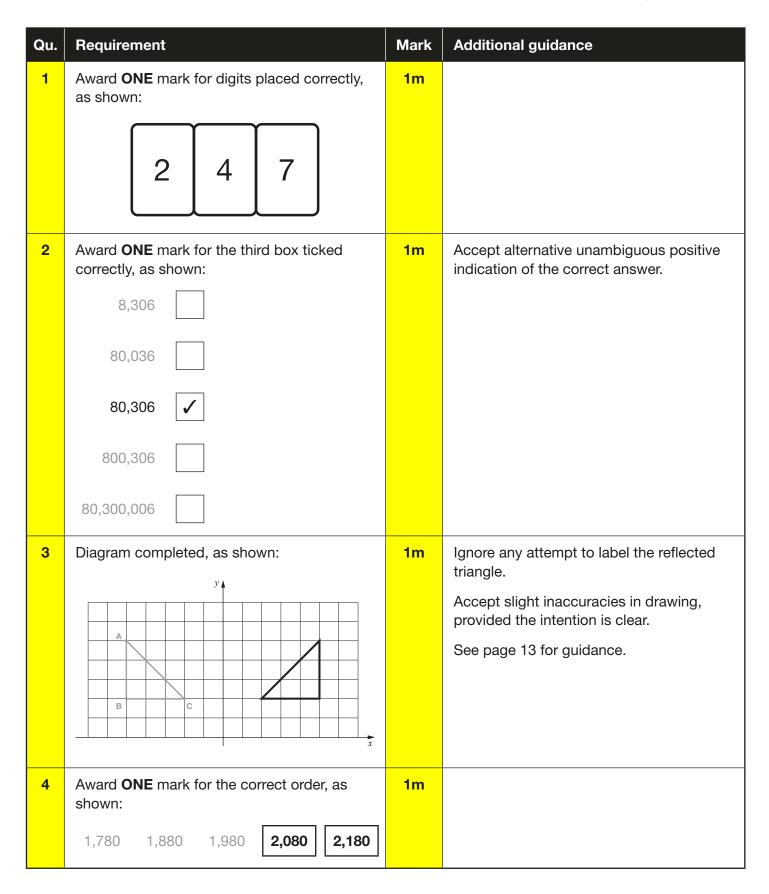
Qu.	Requirement	Mark	Additional guidance
15	All four fractions correctly placed on the number line, as shown:	1m	Misreads are not allowed.
	number line, as shown.		Accept equivalent fractions.
	$\begin{bmatrix} \frac{1}{4} \end{bmatrix} \begin{bmatrix} \frac{1}{2} \end{bmatrix}$		
	$\left[\frac{1}{6}\right]$ $\left[\frac{1}{3}\right]$		
16	5	1m	Refer to section 6.3 on page 16 for
			additional guidance on marking answers involving measures.
17	Award TWO marks for the correct answer of	Up to	
	33	2m	Answer need not be abtained for the
	If the answer is incorrect, award ONE mark for evidence of an appropriate method, e.g.		Answer need not be obtained for the award of ONE mark.
	 4 × 50 = 200 200 ÷ 6 = 30 (error) 		If the pupil reaches an answer with a remainder and subsequently rounds to the
	OR		nearest integer value either side, then the
	• $50 \div 6 = 8 r^2$		method remains appropriate for the award of ONE mark, e.g.
	$(8 r 2) \times 4 = 32 r 8$		• 200 ÷ 6 = 31 r 8
	OR		Acceptable rounded answers would be 31 OR 32
	Award ONE mark for sight of:		For the 'sight of' mark, accept equivalent fractions.
	• 33 ¹ / ₃ OR 33.3 OR 33.33 r OR 33.3		
	OR 33r2		Award ONE mark for an answer of 34.
	(as evidence of completing 200 ÷ 6 correctly without interpreting the remainder in context)		

Qu.	Requirement	Mark	Additional guidance
18	Award TWO marks for the correct answer of $\frac{7}{20}$		Accept for TWO marks for an equivalent fraction of $\frac{7}{20}$ e.g. $\frac{35}{100}$
	If the answer is incorrect, award ONE mark for evidence of an appropriate method, e.g. • $\frac{3}{5} = \frac{3 \times 4}{5 \times 4} = \frac{12}{20}$ $\frac{1}{20} + \frac{12}{20} = \frac{13}{20}$ $1 - \frac{13}{20}$ • $\frac{1}{20} + \frac{3}{5} = \frac{13}{20}$		Answer need not be obtained for the award of ONE mark.
	$1 - \frac{13}{20}$ OR • Award ONE mark for sight of $\frac{13}{20}$ (as evidence of correctly totalling price A and price B tickets).		Also accept for ONE mark equivalent fractions for $\frac{13}{20}$ e.g. $\frac{65}{100}$
19	200	1m	
20	Award TWO marks for boxes completed correctly, as shown: $3 2 3 5$ $\times \underline{53}$ $9 7 0 5$ $\underline{1 6 1 7 5 0}$ $\underline{1 7 1 4 5 5}$ If the answer is incorrect, award ONE mark for either box completed correctly.	Up to 2m	

Qu.	. Requirement		Additional guidance	
21	Award TWO marks for 267.5 OR 267 $\frac{1}{2}$ (cm)			
	If the answer is incorrect, award ONE mark for evidence of an appropriate method, e.g.		Answer need not be obtained for the award of ONE mark.	
	 30 × 8 = 210 (error) 2.5 × 11 = 27.5 210 + 27.5 			
	OR			
	 30 ÷ 2.5 = 12 8 × 12 + 11 = 106 (error) 106 × 2.5 			
	OR			
	 12 inches = 1 ft 1 ft + 8 ft = 9 ft 30 × 9 = 270 270 - 2.5 			
22		1m	1	
~~~	$\frac{3}{12}$		Also accept equivalent fractions, e.g. $\frac{1}{4}$	
23	Award <b>TWO</b> marks for the correct answer of 19	Up to 2m		
	If the answer is incorrect, award <b>ONE</b> mark for evidence of an appropriate method, e.g.		Answer need not be obtained for the award of <b>ONE</b> mark.	
	• $650 \div 10 = 65$ $65 \times 2 = 130$ 650 + 130 = 780 $780 \div 40$		If a pupil's method uses repeated addition or subtraction appropriately, only one step error is allowed, otherwise the method is not appropriate.	
	<ul> <li>20% of 650 = 130</li> <li>130 + 650 = 770 (error)</li> <li>770 ÷ 40</li> </ul>		If the pupil reaches an answer with a remainder and subsequently rounds to the nearest integer value either side, then the	
	OR		method remains appropriate for the award of <b>ONE</b> mark, e.g.	
	Award <b>ONE</b> mark for sight of:			
	<ul> <li>19.5 OR 19¹/₂ OR 19 r20 OR 19 r2</li> </ul>		780 ÷ 40 = 14 r2 ( <i>error</i> )	
	(as evidence of a complete method before rounding down)		Acceptable rounded answers would be 14 <b>OR</b> 15	
			Award <b>ONE</b> mark for an answer of 20.	

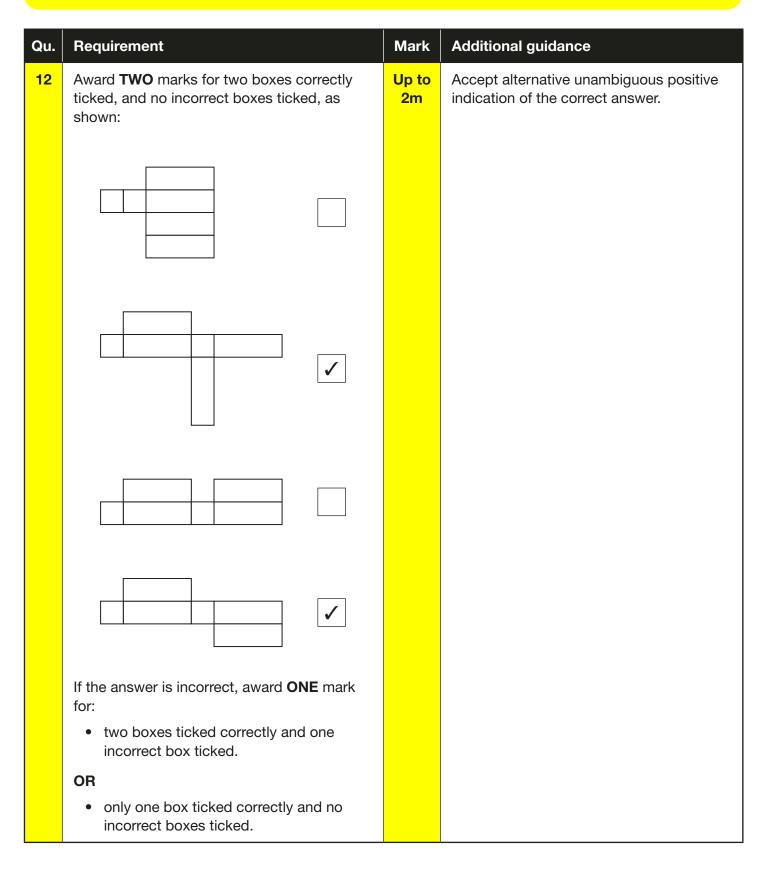
Qu.	Requirement	Mark	Additional guidance	
24	564	1m		
<b>25a</b>	20	1m		
25b	Award <b>TWO</b> marks for the correct answer of 4.8 (g)		Accept for <b>TWO</b> marks 0.0048 kg for final answer in working and the answer box blank <b>OR</b> 0.0048 in answer box where the grams has been replaced with kilograms (kg).	
	If the answer is incorrect, award <b>ONE</b> mark for evidence of an appropriate method, e.g. • $2.4 \times 1000 = 240$ ( <i>error</i> ) $240 \div 500$ • $2.4 \div 500 = 0.0048$ $0.0048 \times 1000$		Accept for <b>ONE</b> mark 0.0048g in the answer box <b>OR</b> as the final answer in the working and answer box blank. Answer need not be obtained for award of <b>ONE</b> mark.	
26a	18	1m		
26b	3	1m		

# 9. Mark schemes for Paper 3: reasoning



Qu.	Requirement	Mark	Additional guidance
5	Correct decimals circled, as shown:           13.2         14.7         15.9         16.3         17.6	1m	Accept alternative unambiguous positive indication of the correct answer.
6	300,000	1m	
7	$10\frac{1}{2}$	1m	Also accept equivalent decimal answers, e.g. 10.5 <b>OR</b> 10.50
8	Award <b>ONE</b> mark for the four shapes matched correctly, as shown:	1m	Lines need not touch the shapes and names, provided the intention is clear.
	irregular pentagon		<b>Do not</b> accept any shape that has been matched to more than one name.
	irregular hexagon		
	regular hexagon		
	regular pentagon		
9	<ul> <li>Award ONE mark for an explanation that recognises that 32 is not a multiple of 3, e.g.</li> <li>32 is not in the 3× table</li> <li>32 ÷ 3 = 10 r2 or 10.66 (which are not whole numbers)</li> </ul>	1m	<b>Do not</b> accept responses that restate the question, e.g. Jack is not correct because if you multiply 3 by any whole number you will not get 32. <b>Do not</b> accept vague or incomplete
	<ul> <li>if you count in multiples of 3 from 0, you won't get 32</li> <li>3 + 2 = 5, 5 is not a multiple of 3 so he is wrong.</li> </ul>		<ul> <li>explanations, e.g.</li> <li>If you multiply by 3 you will get 30, not 32</li> <li>3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33</li> </ul>
	OR		<ul> <li>32 is not a factor of 3</li> </ul>
	<ul> <li>For a description that includes one or both of the multiples of 3 either side of 32, e.g.</li> <li>if you do 10 × 3 = 30 and 11 × 3 = 33 there is no 32</li> <li>10 × 3 = 30 and 32 is 2 away</li> </ul>		<b>Do not</b> accept explanations which include incorrect mathematics or incorrect information relevant to the explanation.
	• 10 × 3 = 30 and 32 is 2 away.		

Qu.	Requirement Mark		Additional guidance
10	3	1m	Accept the answer of 9 as long as the exponent has been crossed out.
11	1     Award TWO marks for correct answer of 2,458     Up 2		
	If the answer is incorrect, award <b>ONE</b> mark for evidence of an appropriate method, e.g.		Answer need not be obtained for the award of <b>ONE</b> mark.
	<ul> <li>7,918 + 4,624 = 12,542</li> <li>15,000 - 12,542</li> </ul>		
	OR		
	<ul> <li>15,000 – 7,918 = 7,182 (error)</li> <li>7,182 – 4,624</li> </ul>		
	OR		
	<ul> <li>15,000 - 4,624 = 10,376</li> <li>10,376 - 7,918 = 2,558 (error)</li> </ul>		



Qu.	Requirement	Mark	Additional guidance
13	9	1m	
<b>14a</b>	$\frac{1}{4}$	1m	<b>Do not</b> accept equivalent fractions.
14b	<u>2</u> 5	1m	Do not accept equivalent fractions.
<b>15</b> a	Award <b>ONE</b> mark for: • 5:50, (0)5:50 pm <b>OR</b> 17:50	1m	Accept answer in words, e.g. ten to six <b>OR</b>
			Answer written unconventionally, e.g. 10 to 6
			Refer to section 6.2 on pages 15 and 16 for additional guidance on marking answers involving a time.
15b	Award <b>ONE</b> mark for: • 1 (hours) 45 (minutes)	1m	Award the mark if the answer is given in hours only or minutes only, i.e.
			<ul> <li>1.75 (hours) Blank (minutes)</li> </ul>
			<ul><li>OR</li><li>Blank (hours) 105 (minutes)</li></ul>
16	Award <b>TWO</b> marks for correct answer of 35(g)	Up to 2m	
	If the answer is incorrect, award <b>ONE</b> mark for evidence of an appropriate method, e.g.		Answer need not be obtained for the award of <b>ONE</b> mark.
	<ul> <li>870 - 30 = 840 840 ÷ 24</li> <li>OR</li> <li>870 - 30 = 850 (error) 250 = 24 = 25 = 120</li> </ul>		If the pupil reaches an answer with a remainder and subsequently rounds to the nearest integer value either side, then the method remains appropriate for the award of <b>ONE</b> mark, e.g.
	850 ÷ 24 = 35 r 10		840 ÷ 24 = 36 r 10
			Acceptable rounded answers would be 36 <b>OR</b> 37
17	<u>5</u> 6	1m	Accept equivalent fractions, e.g. $\frac{10}{12}$

Qu.	Requirement	Mark	Additional guidance
18a	Award <b>ONE</b> mark for drawing the bar in the range of 650 mm to 750 mm, e.g.	1m	Ignore the width of the bar.
	Rainfall at Heathrow Airport		
18b	200 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 +	Up to 2m	Answer need not be obtained or rounded for the award of <b>ONE</b> mark.
	If the answer is incorrect, award <b>ONE</b> mark for evidence of an appropriate method, e.g. • $1,452 + 1,669 + 1,508 = 4,629$ $4,629 \div 3$ <b>OR</b> • $1,452 + 1,669 + 1,508 = 4619$ ( <i>error</i> ) $4619 \div 3$		Any acceptable rounding or truncating does not negate an appropriate method. Any value which does not result from correct rounding or truncating implies an additional step not shown.
	<b>OR</b> Award <b>ONE</b> mark for sight of 4629 (as evidence of the sum of sunshine hours)		

Qu.	. Requirement		Additional guidance
19	Award <b>TWO</b> marks for the correct answer of (£)2.65		Misreads are <b>not</b> allowed.
	If the answer is incorrect, award <b>ONE</b> mark for evidence of a complete method which contains no more than one arithmetic error, e.g. • $\pounds 3.20 \div 2 = \pounds 1.60$ $\frac{1}{4}$ of $60p = 15p$ 60p + 15p = 75p $\pounds 1.60 + 75p = \pounds 2.25$ (error) $\pounds 5 - \pounds 2.25 = \pounds 2.75$ <b>OR</b> • sight of (\pounds)2.35 <b>OR</b> 235 (p) (as evidence of the total cost of mushrooms and carrots).		Accept for <b>ONE</b> mark an answer of £265, £265p or £2,65 as evidence of an appropriate method. Refer to section 6.1 on pages 14 and 15 for additional guidance on marking answers involving money.
20	Award <b>TWO</b> marks for the three correct expressions circled, as shown: $w \times 6$ $w \times 2 + 12$ $6 + w + 6 + w$ Award <b>ONE</b> mark for two correct expressions circled and no incorrect expressions circled.	Up to 2m	Accept alternative unambiguous positive indication of the correct answers.

Qu.	Requirement	Mark	Additional guidance
21	Award <b>THREE</b> marks for the correct answer of 323 Award <b>TWO</b> marks for:		A misread of a number may affect the award of marks. No marks are awarded if there is more than one misread or if the mathematics is simplified.
	• An incorrect answer with evidence of an appropriate complete method with no more than one arithmetic error, e.g.		<b>TWO</b> marks will be awarded if an appropriate method with the misread number is followed through correctly.
	$ \begin{array}{c} 25 \\ \times \underline{34} \\ 100 \\ \underline{750} \\ 950 \ (error) \end{array} $		<b>ONE</b> mark will be awarded for evidence of an appropriate method with the misread number followed through correctly with no more than one error.
	62% of 950 = 589 950 - 589 = 361 <b>OR</b>		Within an appropriate method, if the pupil has rounded appropriately with no more than one arithmetic error, the pupil may be awarded <b>TWO</b> marks.
	<ul> <li>34 × 25 = 950 (error)</li> <li>95 × 3 = 285</li> <li>9.5 × 8 = 76</li> <li>285 + 76 = 361</li> </ul>		
	OR • sight of 527 (as evidence of calculating 62% of 850)		
	<ul><li>Award <b>ONE</b> mark for:</li><li>evidence of an appropriate method with more than one error.</li></ul>		Answer need not be obtained for the award of <b>ONE</b> mark.
	<ul> <li>or sight of 850 (as evidence of the multiplication step completed correctly)</li> </ul>		
22	Number machine boxes completed correctly, as shown:		
	octagon 8 ×5 ÷2 20		

Qu.	Requirement			Mark	Additional guidance
23	Award <b>TWO</b> marks for two correct answers in the boxes, as shown:		Up to 2m		
	а	Ь	a b		
	1	4	0.25		
	3	20	0.15		
	5	8	0.625		
	Award <b>ONE</b> mark for one correct answer.				

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